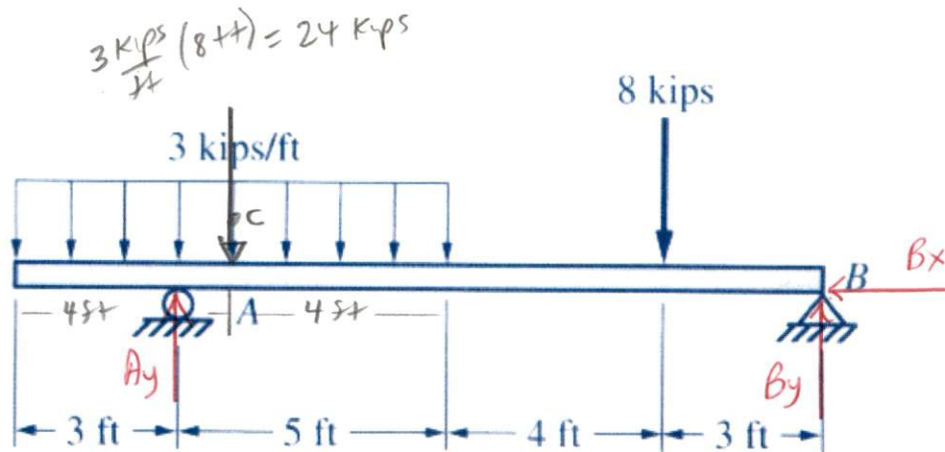


13-30

13-22 to 13-37 Refer to Figs. P13-22 to P13-37. Construct the shear force and the bending moment diagrams for the beam in each figure due to the loading shown by using the relationships among the load, shear, and moment diagrams.



Solution.

FBD

Equilibrium Equations

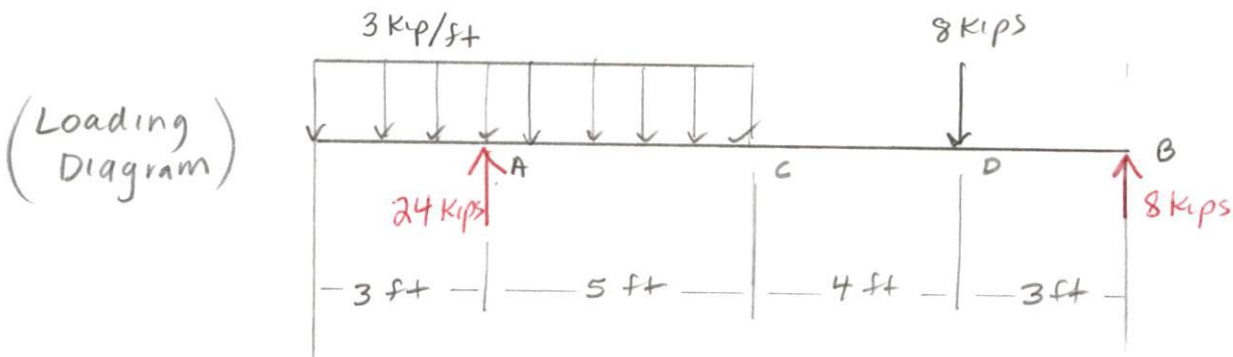
$$[\sum F_x = 0] \quad B_x = 0$$

$$[\sum M_A = 0] \quad -24 \text{ kips} (1 \text{ ft}) - 8 \text{ kips} (9 \text{ ft}) + B_y (12 \text{ ft}) = 0$$

$$B_y = \frac{96 \text{ kip}\cdot\text{ft}}{12 \text{ ft}} = 8 \text{ kips} \uparrow$$

$$[\sum F_y = 0] \quad A_y - 24 \text{ kips} - 8 \text{ kips} + B_y = 0$$

$$A_y = 32 \text{ kips} - 8 \text{ kips} = 24 \text{ kips} \uparrow$$



Shear (kips)

$$V_{A-} = -\frac{3 \text{ kip}}{\text{ft}} (3 \text{ ft}) = -9 \text{ kips}$$

$$V_{A+} = -9 \text{ kips} + 24 \text{ kips} = +15 \text{ kips}$$

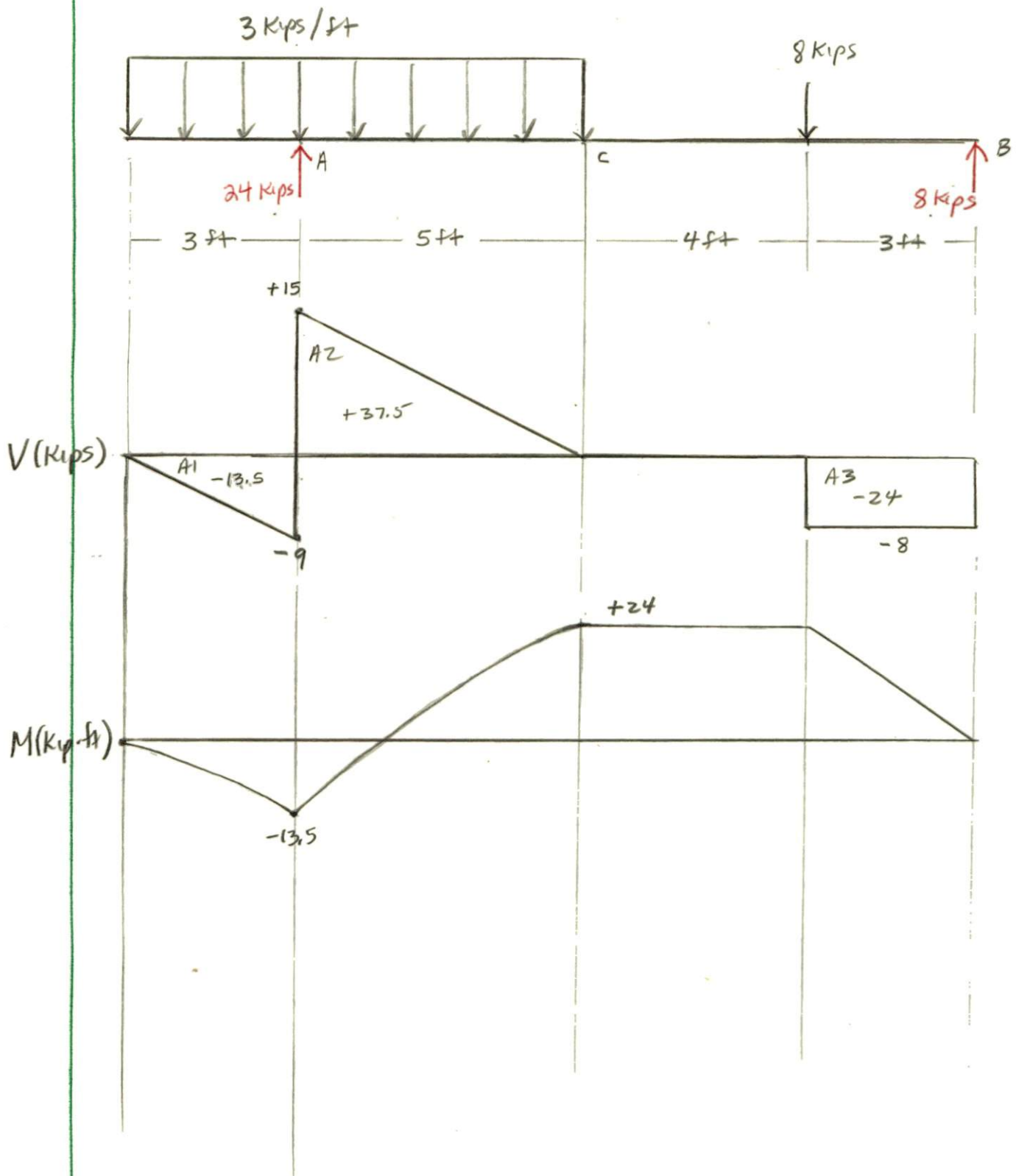
$$V_c = +15 \text{ kips} - 3 \frac{\text{kips}}{\text{ft}} (5 \text{ ft}) = +15 \text{ kips} - 15 \text{ kips} = 0$$

$$V_{D-} = 0$$

$$V_{B-} = -8 \text{ kips}$$

$$V_{D+} = -8 \text{ kips}$$

$$V_{B+} = -8 \text{ kips} + 8 \text{ kips} = 0$$



Internal Bending Moment (area under Shear Curve)

$$A_1 = \frac{1}{2} (3\text{ft}) (-9\text{kips}) = -13.5 \text{ kip}\cdot\text{ft}$$

$$A_2 = \frac{1}{2} (5\text{ft}) (+15\text{kips}) = +37.5 \text{ kip}\cdot\text{ft}$$

$$A_3 = 3\text{ft} (-8\text{kips}) = -24 \text{ kip}\cdot\text{ft}$$