

Solution

CMGT 350

Exam #3

Fall 2020

Show all work for full credit. You may work with ONE other person.

Due: End of Class Today

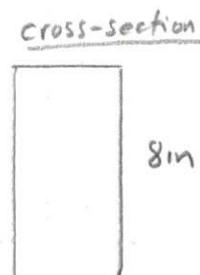
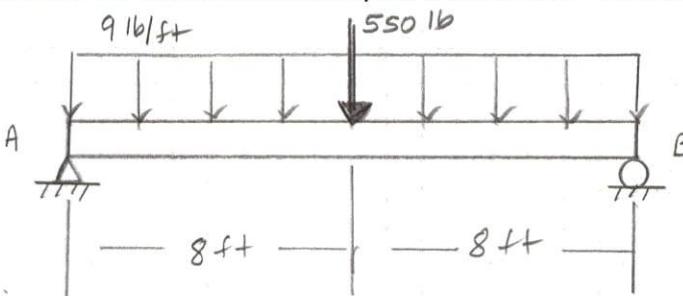
1. A 3-in x 8-in full size rectangular beam has a 16-ft simple span. The beam is subjected a 9 lb/ft uniform load applied to the entire span and a 550 lb concentrated load at midspan. The allowable deflection is 1/360 of the span length. Determine whether the beam is satisfactory for deflection. $E = 1.3 \times 10^3$ ksi

$$P = 550 \text{ lb}$$

$$W = 9 \frac{\text{lb}}{\text{ft}} \left(\frac{\text{ft}}{12 \text{ in}} \right) = 0.75 \frac{\text{lb}}{\text{in}}$$

$$L = 16 \text{ ft} \left(\frac{12 \text{ in}}{1 \text{ ft}} \right) = 192 \text{ in.}$$

$$E = 1300 \text{ ksi}$$



$$I = \frac{bh^3}{12} = \frac{3 \text{ in} (8 \text{ in})^3}{12} = 128 \text{ in}^4$$

Table 16-1, Case 5 and Case 7

Case 5

$$\delta_{\max} = \frac{PL^3}{48EI} = \frac{550 \text{ lb} (192 \text{ in})^3}{48(1,300,000 \text{ psi})(128 \text{ in}^4)} = \frac{3,892,838,400 \text{ in}^3}{7,987,200,000 \text{ in}^2} = 0.487 \text{ in.}$$

Case 7

$$\delta_{\max} = \frac{5WL^4}{384EI} = \frac{5 \left(0.75 \frac{\text{lb}}{\text{in}} \right) (192 \text{ in})^4}{384(1,300,000 \text{ psi})(128 \text{ in}^4)} = \frac{5096079360 \text{ in}^3}{63897600000 \text{ in}^2} = 0.0798 \text{ in}$$

Total Deflection

$$\delta_{\max} = 0.487 \text{ in.} + 0.0798 \text{ in.} = 0.567 \text{ in.}$$

$$\delta_{allow} = \frac{L}{360} = \frac{192 \text{ in.}}{360} = 0.533 \text{ in.}$$

$$\delta_{\max} = 0.567 \text{ in.} > \delta_{allow} = 0.533 \text{ in.}$$

∴ Beam is NOT satisfactory for Deflection.